1 Preferences

Indifference

 $(1,0) \gtrsim (0,1)$ $(0,1) \gtrsim (1,0)$ $(1,0) \sim (0,1)$

Strict Preference

- $(2,0) \succeq (1,0)$
- $(1,0)\not\succsim(2,0)$
- $(2,0) \succ (1,0)$

Best. Something is best from a set if it is weak prefered to everything in the set.

 $a \succsim b, a \succsim c, b \succsim c, a \succsim a, b \succsim b, c \succsim c$

Transitive Relation, Complete.

Rational.

If preference relation is rational, for every set there is at least one best element.

$$\begin{split} & \{a, b, c\} : a \\ & \{b, c\} : b \\ & a \succsim b, b \succsim c, c \succsim a, a \succsim a, b \succsim b, c \succsim c \\ & a \succ b, b \succ c, c \succ a \end{split}$$

Because $a \succeq b, b \succeq c$ but it is not true that $a \succeq c$ this is intransitive.

 $\{a,b,c\}:/?$

 $a \succsim b, a \succsim c, a \succsim a, b \succsim b, c \succsim c$

 \boldsymbol{b} and \boldsymbol{c} are not compared. This is incomplete.

 $\{b, c\}$: ?

We need preferences to be complete and transtiive to use them to represents choice.

1.1 Representing Preferences

1.2 Example

 $a\succsim b,b\succsim c,a\succsim c,a\succsim a,b\succsim b,c\succsim c$

1.3 Example 2

 $\begin{aligned} a \succeq a, a \succeq b, a \succeq c, a \succeq d, a \succeq e \\ b \succeq b, b \succeq a, b \succeq c, b \succeq d, b \succeq e \\ c \succeq c, c \succeq d, c \succeq e \\ d \succeq d, d \succeq c, d \succeq e \\ e \succeq e \end{aligned}$

Directed Graph A graph of preferences has verticies for each thing, and edges that are direct from a to b if $a \succeq b$.

Chain Notation Chain notation puts the objects in a order and uses only \succ, \sim to represent the relationships.

 $a \succeq b, b \succeq c, a \succeq c, a \succeq a, b \succeq b, c \succeq c$

Start with any object.

 $a\succ b\succ c$

 $\begin{aligned} a \gtrsim a, a \gtrsim b, a \gtrsim c, a \gtrsim d, a \gtrsim e \\ b \gtrsim b, b \gtrsim a, b \gtrsim c, b \gtrsim d, b \gtrsim e \\ c \gtrsim c, c \gtrsim d, c \gtrsim e \\ d \gtrsim d, d \gtrsim c, d \gtrsim e \\ e \gtrsim e \end{aligned}$

$$a \sim b \succ c \sim d \succ e$$

Chain notation uses only \succ and \sim and puts bundles/objects in order such that better things are on the left.

$$\begin{split} a \succsim b, b \succsim a, b \succsim c, a \succsim c, a \succsim a, b \succsim b, c \succsim c \\ a \sim b, b \succ c, a \succ c \end{split}$$

 $a \sim b \succ c$

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b \sim a \succ c
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1.4 Exercise 3.3

 $\begin{aligned} a \sim b, a \sim c, b \sim c \\ a \sim b \sim c \end{aligned}$

1.5 Induced Sets

Remy preferes any bowl of ice cream with more scoops regardless of the flavor.

 ${\bf Perfect \ Substitutes \ Preferences}$

$$(2,1) \succeq (1,1)$$

$$(3,0) \succeq (0,2)$$

1.5.1 Indifference Set (Indifference Curve)

 $\sim (1,1)$

All the bundles that are indifferent to (1,1)

1.5.2 Strictly Prefered Set

 $\succ (1,1)$

All of the bundles that are strictly better than (1, 1)

1.5.3 Weakly Prefered Set

 $\succeq (1,1) \Longrightarrow (1,1) \cup \sim (1,1)$

For bundle x the set of weakly prefered bundles $\succsim (x)$ are all of the other bundles y such that :

 $y\succsim x$

$$\succsim (x) = \{y | y \in X, y \succsim x\}$$

 $(1,1) \in \succeq (1,1)$ $(2,2) \in \succeq (1,1)$

1.6 Another Example

Suppose someone only consumes left and right shoes and consumes in pairs. For every left shoe they need a right shoe to make a pair. They only care about the useable pairs of shoes they have.

Perfect Complements Preferences

L-shaped indifference curves (see noets)

1.6.1 Marginal Rate of Substitution

The slope of an indifference curve at some point representes how much x_2 a consumer is willing to give up to get one more unit of x_1 .

We call this the marginal rate of substitution.

If the marginal rate of subtitution is a large negative number, the